Constructing a Parabola: Lesson Plan

Overview:
Students will learn about the rich history of Islamic Mathematics, and will gain an understanding of the relationship of Islamic mathematics to modern mathematics. This unit requires some basic knowledge of geometry, and so is geared towards high school students or middle-school students learning about parabolas and geometrical figures. Students will learn one of the methods used by Muslim mathematicians in constructing parabolas. Using the history intertwined with the mathematics lesson, students will be more interested in the lesson and have a better understanding of parabolas.

Objectives:
Students will be able to:
1. Recount a brief history of Islamic mathematics and the expansion of Greek mathematics in the Arab world
2. Construct a parabola
3. *Optional*: Construct a geometric proof

Activity:
Opening / Hook:
1. Students should be familiar with geometric figures, such as curves and hyperbola.
   Definitions:
   - A **parabola** is the set of all points in the plane equidistant from a given line L (the conic section directrix) and a given point F not on the line (the focus). *Definition from Wolfram MathWorld*
   - A parabola has one **focus** and a **directrix** (line) such that the distance from any point of the parabola to the focus is equal to the (perpendicular) distance from the point to the directrix. *from Wikipedia, focus*
   - The **axis** of the parabola passes through the focus and is perpendicular to the directrix.

Introduce New Material:
1. First, show parabolas drawn on the board, showing its vertex, axis, and parameter, which is the distance from vertex to the focus, or vertex to the directrix (by definition of the focus, this distance is equal). Also provide its equation, with vertex (x, h) and parameter p, in the forms:
   $(x-h)^2 = 4p(y-k)$ – where the parabola's axis is parallel to the x-axis
   $(y-k)^2 = 4p(x-h)$ – where the parabola's axis is parallel to the y-axis
   You may wish to use the following examples: