

# TRIGONOMETRIC FUNCTION IDENTITIES

<b>Quotient Identities</b>	<b>Reciprocal Identities</b>
$\tan\theta = \frac{\sin\theta}{\cos\theta}$ $\cot\theta = \frac{\cos\theta}{\sin\theta}$	$\sin\theta = \frac{1}{\csc\theta}$ $\csc\theta = \frac{1}{\sin\theta}$ $\cos\theta = \frac{1}{\sec\theta}$ $\sec\theta = \frac{1}{\cos\theta}$ $\tan\theta = \frac{1}{\cot\theta}$ $\cot\theta = \frac{1}{\tan\theta}$
<b>Pythagorean Identities</b>	<b>Even/Odd Identities</b>
$\sin^2\theta + \cos^2\theta = 1$ $\sec^2\theta - \tan^2\theta = 1$ $\csc^2\theta - \cot^2\theta = 1$	$\sin(-\theta) = -\sin\theta$ $\cos(-\theta) = \cos\theta$ $\tan(-\theta) = -\tan\theta$ $\cot(-\theta) = -\cot\theta$ $\csc(-\theta) = -\csc\theta$ $\sec(-\theta) = \sec\theta$
<b>Cofunction Identities</b>	<b>Sum/Difference Identities</b>
$\sin\left(\frac{\pi}{2} - \theta\right) = \cos\theta$ $\cos\left(\frac{\pi}{2} - \theta\right) = \sin\theta$ $\tan\left(\frac{\pi}{2} - \theta\right) = \cot\theta$ $\cot\left(\frac{\pi}{2} - \theta\right) = \tan\theta$ $\csc\left(\frac{\pi}{2} - \theta\right) = \sec\theta$ $\sec\left(\frac{\pi}{2} - \theta\right) = \csc\theta$ $\frac{\pi}{2}$ radians = $90^\circ$	$\sin(\theta \pm \phi) = \sin\theta \cos\phi \pm \cos\theta \sin\phi$ $\cos(\theta \pm \phi) = \cos\theta \cos\phi \mp \sin\theta \sin\phi$ $\tan(\theta \pm \phi) = \frac{\tan\theta \pm \tan\phi}{1 \mp \tan\theta \tan\phi}$
<b>Double Angle Identities</b>	<b>Half Angle Identities</b>
$\sin(2\theta) = 2 \sin\theta \cos\theta$ $\cos(2\theta) = \cos^2\theta - \sin^2\theta$ $\cos(2\theta) = 2 \cos^2\theta - 1$ $\cos(2\theta) = 1 - 2 \sin^2\theta$ $\tan(2\theta) = \frac{2 \tan\theta}{1 - \tan^2\theta}$	$\sin^2\theta = \frac{1 - \cos(2\theta)}{2}$ $\cos^2\theta = \frac{1 + \cos(2\theta)}{2}$ $\tan^2\theta = \frac{1 - \cos(2\theta)}{1 + \cos(2\theta)}$
<b>Sum to Product of Two Angles</b>	<b>Product to Sum of Two Angles</b>
$\sin\theta + \sin\phi = 2\sin\left(\frac{\theta + \phi}{2}\right)\cos\left(\frac{\theta - \phi}{2}\right)$ $\sin\theta - \sin\phi = 2\cos\left(\frac{\theta + \phi}{2}\right)\sin\left(\frac{\theta - \phi}{2}\right)$ $\cos\theta + \cos\phi = 2\cos\left(\frac{\theta + \phi}{2}\right)\cos\left(\frac{\theta - \phi}{2}\right)$ $\cos\theta - \cos\phi = -2\sin\left(\frac{\theta + \phi}{2}\right)\sin\left(\frac{\theta - \phi}{2}\right)$	$\sin\theta \sin\phi = \frac{[\cos(\theta - \phi) - \cos(\theta + \phi)]}{2}$ $\cos\theta \cos\phi = \frac{[\cos(\theta - \phi) + \cos(\theta + \phi)]}{2}$ $\sin\theta \cos\phi = \frac{[\sin(\theta + \phi) + \sin(\theta - \phi)]}{2}$ $\cos\theta \sin\phi = \frac{[\sin(\theta + \phi) - \sin(\theta - \phi)]}{2}$