

Problem 8. Use vectors to show that the diagonals of a rhombus are perpendicular.
Recall that a rhombus is a parallelogram with sides of equal length.

Problem 9. Consider the quadrilateral in the plane with vertices
 $(-6, 0)$, $(1, -4)$, $(3, 1)$ and $(-4, 5)$.
Show that this quadrilateral is a parallelogram and find its area.

Problem 10. Find the volume of the tetrahedron with vertices
 $(0, 0, 0)$, $(1, 1, 0)$, $(0, 1, 1)$ and $(1, 0, 1)$.

Problem 11. Find the distance from the point $(0, 0, 1)$ to the line
 $x = 2t$, $y = 1 + 2t$, $z = 2t$.

Problem 12. Find the distance from the point $(2, 2, 3)$ to the plane $2x + y + 2z = 4$.

Problem 13. Find a plane through the points $(1, 2, 3)$ and $(3, 2, 1)$ which is
perpendicular to the plane $4x - y + 2z = 7$.

Problem 14. Carefully draw the surface $x^2 + y^2 - z^2 = 1$, including its intersections
with the coordinate planes.

Problem 15. Carefully draw the surface $z = 4x^2 + y^2$, including its intersections with
the coordinate planes.

Problem 16. (a) Using cylindrical coordinates, sketch the surface $z = r^2$.
(b) Using cylindrical coordinates, sketch the surface $r^2 + z^2 = 1$.

Problem 17. (a) Using spherical coordinates, sketch the surface $\cos \phi = \rho \sin^2 \phi$.
(b) Using spherical coordinates, sketch the surface $\rho \cos \phi + \rho^2 \sin^2 \phi = 1$.

Problem 18. In the yz -plane, the circle with center at $y = 2$, $z = 0$ and radius 1 is
rotated about the z -axis to form a donut shaped surface (called a "torus").
Carefully sketch this surface, and then find its equation in cylindrical
coordinates and its equation in spherical coordinates.

*Note. Use a full page for each sketch, make the sketches very clear and not too light,
and use shading to suggest three-dimensionality.*