

In Exercises 45–70, find the derivative of the function.

45.  $g(x) = \ln x^2$

46.  $h(x) = \ln(2x^2 + 1)$

47.  $y = (\ln x)^4$

48.  $y = x \ln x$

49.  $y = \ln(x\sqrt{x^2 - 1})$

50.  $y = \ln \sqrt{x^2 - 4}$

51.  $f(x) = \ln\left(\frac{x}{x^2 + 1}\right)$

52.  $f(x) = \ln\left(\frac{2x}{x + 3}\right)$

53.  $g(t) = \frac{\ln t}{t^2}$

54.  $h(t) = \frac{\ln t}{t}$

55.  $y = \ln(\ln x^2)$

56.  $y = \ln(\ln x)$

57.  $y = \ln \sqrt{\frac{x+1}{x-1}}$

58.  $y = \ln \sqrt{\frac{x-1}{x+1}}$

59.  $f(x) = \ln\left(\frac{\sqrt{4+x^2}}{x}\right)$

60.  $f(x) = \ln(x + \sqrt{4+x^2})$

61.  $y = \frac{-\sqrt{x^2 + 1}}{x} + \ln(x + \sqrt{x^2 + 1})$

62.  $y = \frac{-\sqrt{x^2 + 4}}{2x^2} - \frac{1}{4} \ln\left(\frac{2 + \sqrt{x^2 + 4}}{x}\right)$

63.  $y = \ln|\sin x|$

64.  $y = \ln|\csc x|$

65.  $y = \ln\left|\frac{\cos x}{\cos x - 1}\right|$

66.  $y = \ln|\sec x + \tan x|$

67.  $y = \ln\left|\frac{-1 + \sin x}{2 + \sin x}\right|$

68.  $y = \ln \sqrt{1 + \sin^2 x}$

69.  $f(x) = \sin 2x \ln x^2$

70.  $g(x) = \int_1^{\ln x} (t^2 + 3) dt$