Worksheet on Boolean Algebra Proofs

Prove each of the following by quoting properties of set operations from the text.

1. For all sets A, B and C with elements from the universe U,

$$(A \cap C') \cup (B' \cap C)' = B \cup C'$$

2. For all sets $A,\,B$ and C with elements from the universe U,

$$(A\cap B\cap C)\cup (A\cap B\cap C')\cup (A\cap B'\cap C)\cup (A\cap B'\cap C')=A$$

3. For all sets A, B and C with elements from the universe U, if $A \cup B' = C$, then

$$(A \cap C') \cup (A \cap B')' \cup (A' \cap B)' = C$$

Prove each of the following by quoting properties of a Boolean algebra from the text.

- 1. For all a and b, ab + b + (a' + b)' = a + b.
- 2. For all a, b and c, ab' + a(b' + c)' = a(bc)'.
- 3. For all a, b and c, if a + b = b, then ab + ac(b + c') = a.

Now go to

 ${\rm http://www.ship.edu/\tilde{}-} deensl/DiscreteMath/boolean$ proof solutions.pdf to see one possible solution.