

Magnetic Fields & Force

1. A point charge, $q = 5 \times 10^{-6} \text{ C}$ and $m = 1 \times 10^{-3} \text{ kg}$, travels with a velocity of: $\vec{v} = 30 \frac{\text{m}}{\text{s}} \hat{i}$ then enters a magnetic field: $\vec{B} = 1 \times 10^{-6} \text{ T } \hat{j}$.

a. What is the kinetic energy of the point charge?

Ans. $K = \frac{1}{2}mv^2 = 0.45 \text{ J}$

b. What is the magnitude of the magnetic force that acts on the charge once it has entered the field?

Ans. $|\vec{F}_B| = qvB = 1.5 \times 10^{-10} \text{ N}$

c. What is the magnetic force vector exerted on the charge just as it enters the field?

Ans. $\vec{F}_B = q\vec{v} \times \vec{B} = 1.5 \times 10^{-10} \text{ N } \hat{k}$

d. Why does the magnetic force exerted on the point charge not change its kinetic energy?

Ans. The magnetic force is always to the direction of travel.

2. Initially at rest, a charged particle, $q = +1.6 \times 10^{-19} \text{ C}$ and $m = 1.67 \times 10^{-27} \text{ kg}$, is accelerated through a region of constant electric field ($\vec{E} = E_y \hat{j}$), across a potential difference of $V = 100 \text{ V}$. The charged particle then enters a magnetic field: $\vec{B} = 10^{-3} \text{ T } \hat{i}$.

a. What is the kinetic energy of the particle just as it enters the magnetic field? *Apply the Conservation of Energy to the particle.*

Ans. $K = \Delta K = \Delta U = q\Delta V = 1.6 \times 10^{-17} \text{ J}$

b. Determine the magnetic force vector exerted on the charge, in component form, as it enters the field?

Ans. $v = \sqrt{\frac{2K}{m}} = 1.38 \times 10^5 \frac{\text{m}}{\text{s}} \Rightarrow \vec{F}_B = q\vec{v} \times \vec{B} = -2.21 \times 10^{-17} \text{ N } \hat{k}$

c. In which direction is the particle deflected once it enters the field? Calculate the radius of the particles path.

Ans. Clockwise