

A. Reciprocal

$$\csc = \frac{1}{\sin} \quad \sin \csc = 1$$

$$\sec = \frac{1}{\cos} \quad \cos \sec = 1$$

$$\cot = \frac{1}{\tan}$$

$$\sin = \frac{1}{\csc}$$

$$\cos = \frac{1}{\sec}$$

$$\tan = \frac{1}{\cot}$$

B. Ratio

$$\tan = \frac{\sin}{\cos}$$

$$\cot = \frac{\cos}{\sin}$$

$$\cos = \frac{\sin}{\tan}$$

$$\sin = \frac{\cos}{\cot}$$

$$\sin = \cos \tan$$

$$\cos = \sin \cot$$

C. Pythagorean

$$\sin^2 + \cos^2 = 1$$

$$\tan^2 + 1 = \sec^2$$

$$1 + \cot^2 = \csc^2$$

$$1 - \cos^2 = \sin^2$$

$$1 - \sin^2 = \cos^2$$

$$\sec^2 - 1 = \tan^2$$

$$\sec^2 - \tan^2 = 1$$

$$\csc^2 - 1 = \cot^2$$

$$\csc^2 - \cot^2 = 1$$