

3 THEOREM Suppose \mathbf{u} and \mathbf{v} are differentiable vector functions, c is a scalar, and f is a real-valued function. Then

$$1. \frac{d}{dt} [\mathbf{u}(t) + \mathbf{v}(t)] = \mathbf{u}'(t) + \mathbf{v}'(t)$$

$$2. \frac{d}{dt} [c\mathbf{u}(t)] = c\mathbf{u}'(t)$$

$$3. \frac{d}{dt} [f(t)\mathbf{u}(t)] = f'(t)\mathbf{u}(t) + f(t)\mathbf{u}'(t)$$

$$4. \frac{d}{dt} [\mathbf{u}(t) \cdot \mathbf{v}(t)] = \mathbf{u}'(t) \cdot \mathbf{v}(t) + \mathbf{u}(t) \cdot \mathbf{v}'(t)$$

$$5. \frac{d}{dt} [\mathbf{u}(t) \times \mathbf{v}(t)] = \mathbf{u}'(t) \times \mathbf{v}(t) + \mathbf{u}(t) \times \mathbf{v}'(t)$$

$$6. \frac{d}{dt} [\mathbf{u}(f(t))] = f'(t)\mathbf{u}'(f(t)) \quad (\text{Chain Rule})$$