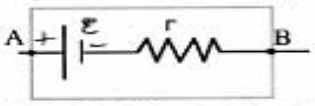
Battery Equivalent Circuit

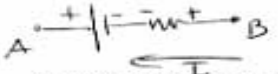
We typically treat a battery as a source of constant voltage, constant potential difference, but battery terminals, in fact, have different potential differences depending on the circuit they are part of.
The diagram below shows a simple way to think about how a power supply / battery acts.



start @ B & add/subtract V's to get to A
$\rightarrow V_B \pm Ir + \mathcal{E} = V_A$

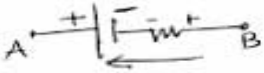
(a) Write an equation for the terminal potential difference $V_A - V_B$ when there is **no current** flowing. when $I = 0$, voltage across $r = Ir = 0$
So $V_A - V_B = +\mathcal{E}$

(b) Write an equation for the terminal potential difference $V_A - V_B$ when the current flows to the **left** in the diagram above.



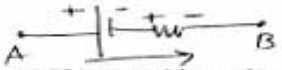
$V_B - Ir + \mathcal{E} = V_A$ $\quad V_A - V_B = \mathcal{E} - Ir$

(c) Write an equation for the terminal potential difference $V_B - V_A$ when the current flows to the **left** in the diagram above.



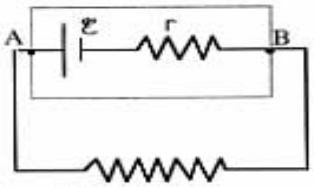
$V_B - V_A = -(V_A - V_B) = -(\mathcal{E} - Ir)$

(d) Write an equation for the terminal potential difference $V_A - V_B$ when the current flows to the **right** in the diagram above.



$V_B + Ir + \mathcal{E} = V_A$
$V_A - V_B = \mathcal{E} + Ir$

(e) Now consider a circuit which consists of a variable resistor R connected across this battery. Let's define the terminal potential difference $V = V_A - V_B$.

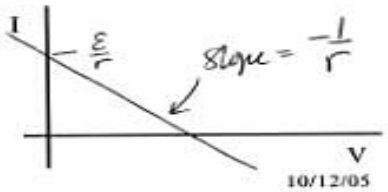


(i) How is the terminal potential difference related to the voltage across R?
$V = V_A - V_B = IR$ = voltage across R

(ii) Write an equation for the current through R as a function of $\mathcal{E}$, r, and V.
$I = \frac{\mathcal{E}}{R_{tot}} = \frac{\mathcal{E}}{R+r}$ & $R = \frac{V}{I}$ so $I = \frac{\mathcal{E}}{\frac{V}{I} + r}$ → algebra

(iii) Sketch a graph that you would expect to get if you plot I (current) as a function of V (voltage) as R is varied.

algebra
$I\left(\frac{V}{I} + r\right) = \mathcal{E}$
$V + Ir = \mathcal{E}$
$I = \frac{\mathcal{E}}{r} - \frac{V}{r} = -\frac{1}{r}(V) + \frac{\mathcal{E}}{r}$
"y" "m" "x" + "b"
negative slope
positive y-intercept



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