



Factoring

SPECIAL PRODUCTS

Perfect Squares

$$(a + b)^2 = a^2 + 2ab + b^2; \quad (a - b)^2 = a^2 - 2ab + b^2$$

Difference of Squares

$$a^2 - b^2 = (a + b)(a - b)$$

Sum of Cubes

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

Difference of Cubes

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

EQUIVALENCES

Factoring Out -1

$$b - a = -(a - b)$$

Commutative Law of Addition

$$a + b = b + a$$

Reversing Differences

$$(b - a)^n = (a - b)^n \text{ when } n \text{ is even, and}$$

$$(b - a)^n = -(a - b)^n \text{ when } n \text{ is odd}$$

COMMON ERRORS

$$(a + b)^2 \neq a^2 + b^2$$

$$(a - b)^2 \neq a^2 - b^2$$

$$(a + b)^2 \neq a^2 + b^2$$

$$(a - b)^2 \neq a^2 - b^2$$

$a^2 + b^2$ is not factorable. See "Special Products" above for the details of how to deal with these expressions.

EXERCISES

A. Factor out the greatest common factor:

1) $8t + 8$

6) $-7y^2 + 21y^2 - 7$

2) $5w - 35$

7) $r^3a - ar^3$

3) $-4h - 4k$

8) $2y(3y - 2) - (3y - 2)$

4) $m^2 - 8m$

9) $3x^2(2x - 1) - 6(1 - 2x)$

5) $-x^2 - x$

10) $5(4 - y) - b(y - 4)$