Exponent Properties

1. Product of like bases:

$$a^m a^n = a^{m+n}$$

To multiply powers with the same base, add the exponents and keep the common base. Example: $x^5x^3 = x^{5+3} = x^8$

Example:
$$x^{5}x^{3} = x^{5+3} = x^{8}$$

$$\frac{a^m}{a^n} = a^{m-n}$$

2. Quotient of like bases: $\frac{a^m}{a^n} = a^{m-n}$ To divide powers with the same base, subtract the exponents and keep the common base. $Example: \frac{x^5}{x^3} = x^{5-3} = x^2$

Example:
$$\frac{x^5}{x^3} = x^{5-3} = x^2$$

3. Power to a power:

$$(a^m)^n = a^{mn}$$

To raise a power to a power, keep the base and multiply the exponents.

Example:
$$(x^5)^3 = x^{5*3} = x^{15}$$

4. Product to a power:

$$(ab)^m = a^m b^m$$

To raise a product to a power, raise each factor to the power.

Example:
$$(x^4y^5)^3 = x^{12}y^{15}$$

5. Quotient to a power

$$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$$

Quotient to a power $\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$ To raise a quotient to a power, raise the numerator and the denominator to the power.

Example:
$$\left(\frac{x^3}{y^2}\right)^4 = \frac{x^{12}}{y^8}$$

6. Zero Exponent:

$$a^{0} =$$

Any number raised to the zero power is equal to "1". Example: $(8x^4)^0$ 1

Example:
$$(8x^4)^0 = 1$$

7. Negative exponent:

$$a^{-n} = \frac{1}{a^n}$$
 or $\frac{1}{a^{-n}} = a$

Negative exponent: $a^{-n} = \frac{1}{a^n}$ or $\frac{1}{a^{-n}} = a^n$ Negative exponents indicate reciprocation, with the exponent of the reciprocal becoming positive. You may want to think of it this way: unhappy (negative) exponents will become happy (positive) by having the base/exponent pair "switch floors"! $Example: 8^{-2} = \frac{1}{8^2} = \frac{1}{64} \qquad or \qquad \frac{4}{x^{-3}} = 4x^3$

Example:
$$8^{-2} = \frac{1}{8^2} = \frac{1}{64}$$

$$\frac{4}{v^{-3}} = 4x$$